



Compiler Design

Syntax Analysis

Introduction to LR Parsing

Simple LR

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Outline

- Why LR parsers?
- Items and the LR(0) Automaton
- The LR Parsing Algorithm
- Constructing SLR Parsing Tables
- Viable Prefixes

Introduction

- LR(k) – the most prevalent type of bottom-up parser
- L – from left to right
- R – constructing the rightmost derivation in reverse
- k - the number of lookahead input symbols
- k=0, k=1 cases are of practical interest
- we consider $k \leq 1$
- when k is omitted then $k=1$

Introduction

- basic concepts of LR parsing
- the easiest method to construct shift-reduce parsers – simple LR (SLR)
- usually LR parsers are built by automatic generators
- “items”
- “parser states”
- next section presents
 - canonical LR
 - LALR
 - complex methods used in the majority of LR parsers

Why LR Parsers ?

- table driven
 - like non-recursive LL parsers
- LR grammar
 - a grammar for which we can use the methods in this section
- is named intuitively
 - a left to right shift-reduce parser
 - to recognize handles of right sentential forms
 - when they appear on the top of the stack

Why LR Parsing ?

- LR parsers can recognize all language constructs written in context free grammars
- the most general non-backtracking shift-reduce parsing method
- can be implemented as efficiently as other more primitive shift-reduce methods
- can detect syntactic error as soon as possible
- the class of LR grammars is a superset of LL or predictive grammars
- too much work to write a LR parser by hand for a typical programming language grammar

Items and LR(0) Automaton

- LR(0) item – production of G with a dot as some point at some position of the body
- production $A \rightarrow XYZ$ yields four items
 - $A \rightarrow \cdot XYZ$
 - $A \rightarrow X \cdot YZ$
 - $A \rightarrow XY \cdot Z$
 - $A \rightarrow XYZ \cdot$
- production $A \rightarrow \epsilon$
 - $A \rightarrow \cdot$

Items

- indicates how much of a production we have seen at a given point in the parsing process
- item $A \rightarrow \bullet XYZ$
 - we hope to see a string derivable from XYZ next on input
- item $A \rightarrow X \bullet YZ$
 - we have just seen a string derivable from X
 - we hope to see a string derivable from YZ next on input
- item $A \rightarrow XYZ \bullet$
 - we have just seen a string derivable from XYZ
 - it may be time to reduce XYZ to A

Representing Item Sets

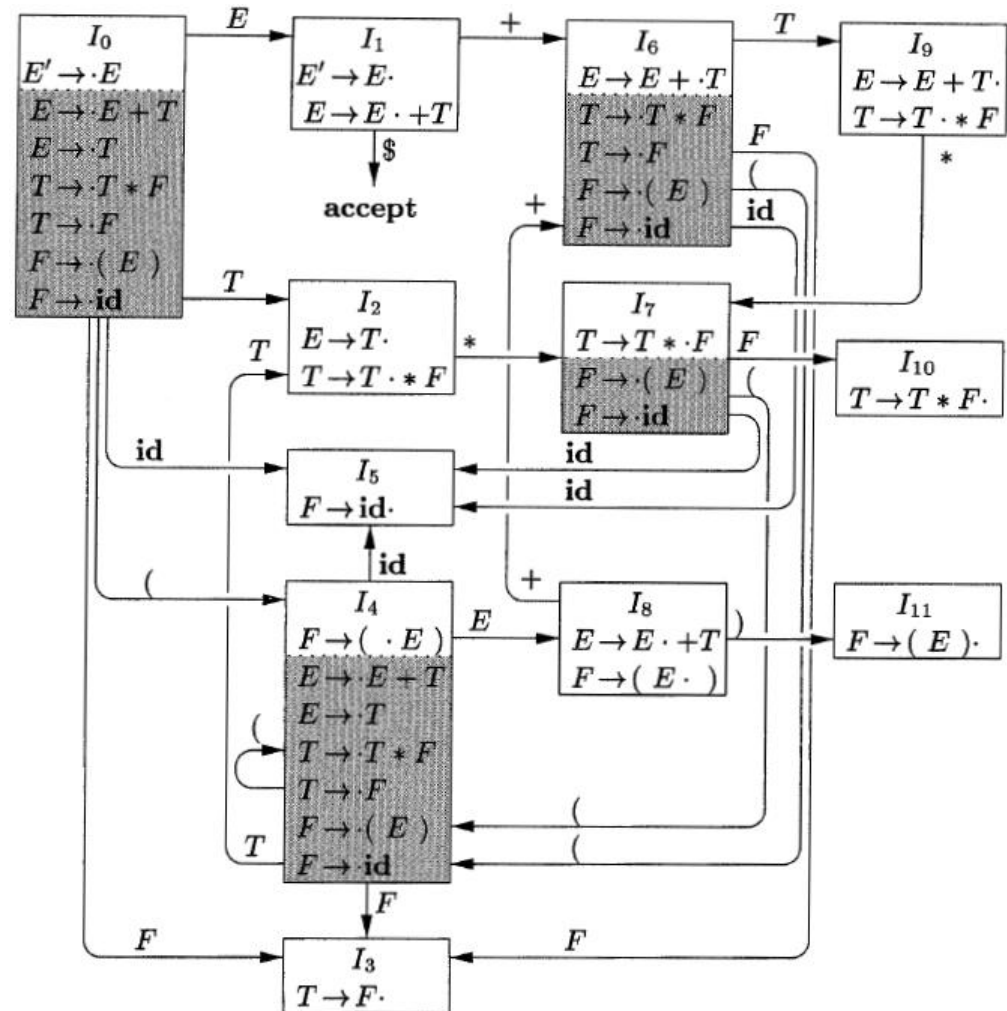
- pair of integers
 - the number of the production
 - the position of the dot
- sets of items
 - lists of such pairs
- closure items
 - the dot is at the beginning of the body
 - can be reconstructed from other items in the set
 - we do not have to include them in the list

Canonical LR(0)

- one collection of sets of LR(0) items
- provides the basis for constructing a DFA
- DFA is used to make parsing decisions
- LR(0) automaton
 - each state of LR(0) – set of items in the canonical LR(0) collection
 - the dead state is not represented !!!
- to build canonical LR(0) means to define
 - an augmented grammar
 - G - grammar with starting symbol S
 - G' – augmented grammar for G, $S' \rightarrow S$
 - acceptance when $S' \rightarrow S$
 - two functions
 - CLOSURE
 - GOTO

LR(0) DFA Example

- $E \rightarrow E + T \mid T$
- $T \rightarrow T * F \mid F$
- $F \rightarrow \text{id} \mid (E)$



Closure of Item Sets

- I is the set of items for grammar G
- $CLOSURE(I)$ – set of items built from I
 - (1) initially add every item I to $closure(I)$
 - (2) if $A \rightarrow \alpha \bullet B \beta$ is in $CLOSURE(I)$ and $B \rightarrow \gamma$
 - then add $B \rightarrow \bullet \gamma$ to $CLOSURE(I)$ if not already there
 - apply this rule until no more new items can be added to $CLOSURE(I)$

Explanations

- $A \rightarrow \alpha \cdot B \beta$ is in $\text{CLOSURE}(I)$
- we might see a substring derivable from $B\beta$ as input
- the string derivable from $B\beta$
 - will have a prefix derivable from B applying one of the B -productions
- if $B \rightarrow \gamma$
 - then we include $B \rightarrow \cdot \gamma$ in $\text{CLOSURE}(I)$

Augmented Expression Grammar

- $E' \rightarrow E$
- $E \rightarrow E+T \mid T$
- $T \rightarrow T*F \mid F$
- $F \rightarrow \text{id} \mid (E)$
- if I is the set of one item $\{[E' \rightarrow \bullet E]\}$
 - then $\text{CLOSURE}\{I\}$ contains the set items of I_0
 - $E' \rightarrow \bullet E$
 - since $E \rightarrow E+T$ and $E \rightarrow T$ we also add
 - $E \rightarrow \bullet E+T$ and $E \rightarrow \bullet T$
 - since $T \rightarrow T*F$ and $T \rightarrow F$ we also add
 - $T \rightarrow \bullet T*F$ and $T \rightarrow \bullet F$
 - since $F \rightarrow (E)$ and $F \rightarrow \text{id}$ we also add
 - $F \rightarrow \bullet (E)$ and $F \rightarrow \bullet \text{id}$

Computation of CLOSURE

SetOfItems CLOSURE(I)

{

 J=I;

repeat

for(each item $A \rightarrow \alpha \bullet B \beta$ in J)

for(each production $B \rightarrow \gamma$ of G)

if($B \rightarrow \bullet \gamma$ is not in J)

 add $B \rightarrow \bullet \gamma$ to J;

until no more items are added to J on one round;

return J;

}

Kernel and Non-kernel Items

- Kernel Items
 - $S' \rightarrow \bullet S$
 - all items whose dots are not at the left end
- Non-kernel Items
 - all items with their dots at the left end
 - Except $S' \rightarrow \bullet S$
- each set is formed by
 - taking the closure of a set of kernel items
 - the items added to the closure can never be kernel items
 - they must not be stored since they can be regenerated



Bibliography

- Alfred V. Aho, Monica S. Lam, Ravi Sethi, Jeffrey D. Ullman – Compilers, Principles, Techniques and Tools, Second Edition, 2007